

$$f(x) = 3 + 4x - x^2$$

1A Find the vertex

Put it in vertex form $\rightarrow y - k = a(x - h)^2$

$$y = 3 + 4x - x^2$$

$$y - 3 = -x^2 + 4x$$

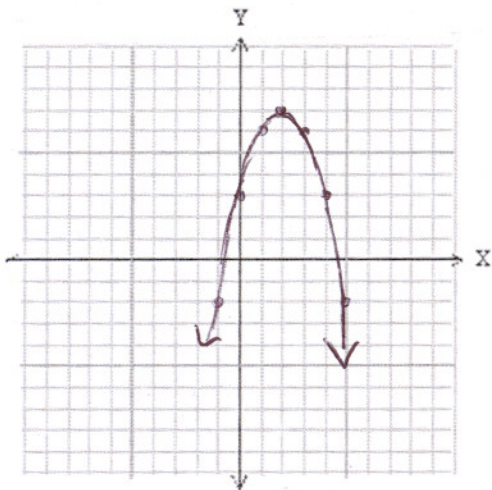
$$y - 3 = -(x^2 - 4x)$$

$$y - 3 - 4 = -(x^2 - 4x + 4)$$

$$y - 7 = -(x - 2)^2$$

vertex is (2, 7)

1B Find the domain and range



1) make a rough sketch

2) put vertex on graph (h, k)

3) look at a to determine if graph

looks like  or 

4) Domain is all real numbers

(you can go as far left & right as you wish)

5) Range if maximum $y \leq k$

Range if minimum $y \geq k$

Domain: All real #'s

Range: $y \leq 7$

C Find the zeros

Let's go back to the original equation and set $f(x) = 0$

$$f(x) = 3 + 4x - x^2$$

$$\downarrow$$
$$0 = 3 + 4x - x^2 \quad \text{OR} \quad \boxed{-x^2 + 4x + 3 = 0}$$

Looks like a job for the quadratic formula!

$$a = -1 \quad b = 4 \quad c = 3$$

$$x = \frac{-(4) \pm \sqrt{(4)^2 - 4(-1)(3)}}{2(-1)}$$

$$x = \frac{-4 \pm \sqrt{16 + 12}}{-2}$$

$$x = \frac{-4 \pm \sqrt{28}}{-2}$$

$$x = \frac{-4}{-2} \pm \frac{2\sqrt{7}}{-2}$$

$$x = 2 \pm \sqrt{7}$$